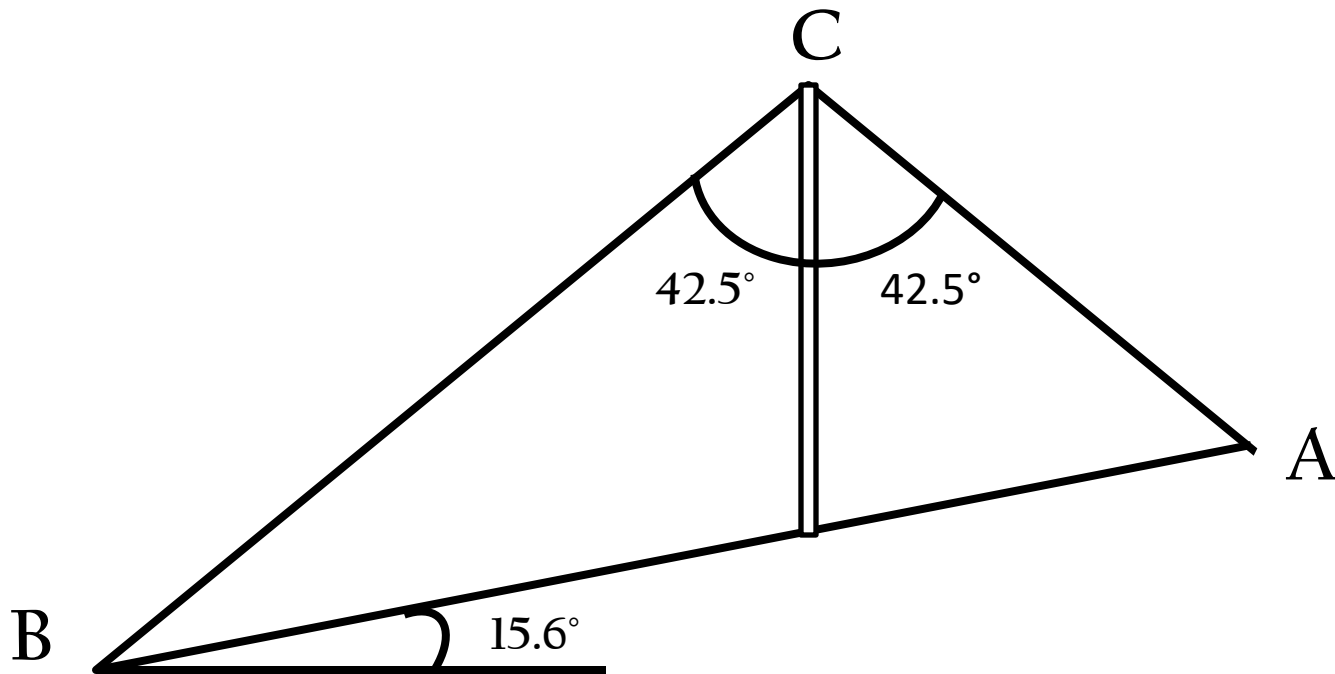
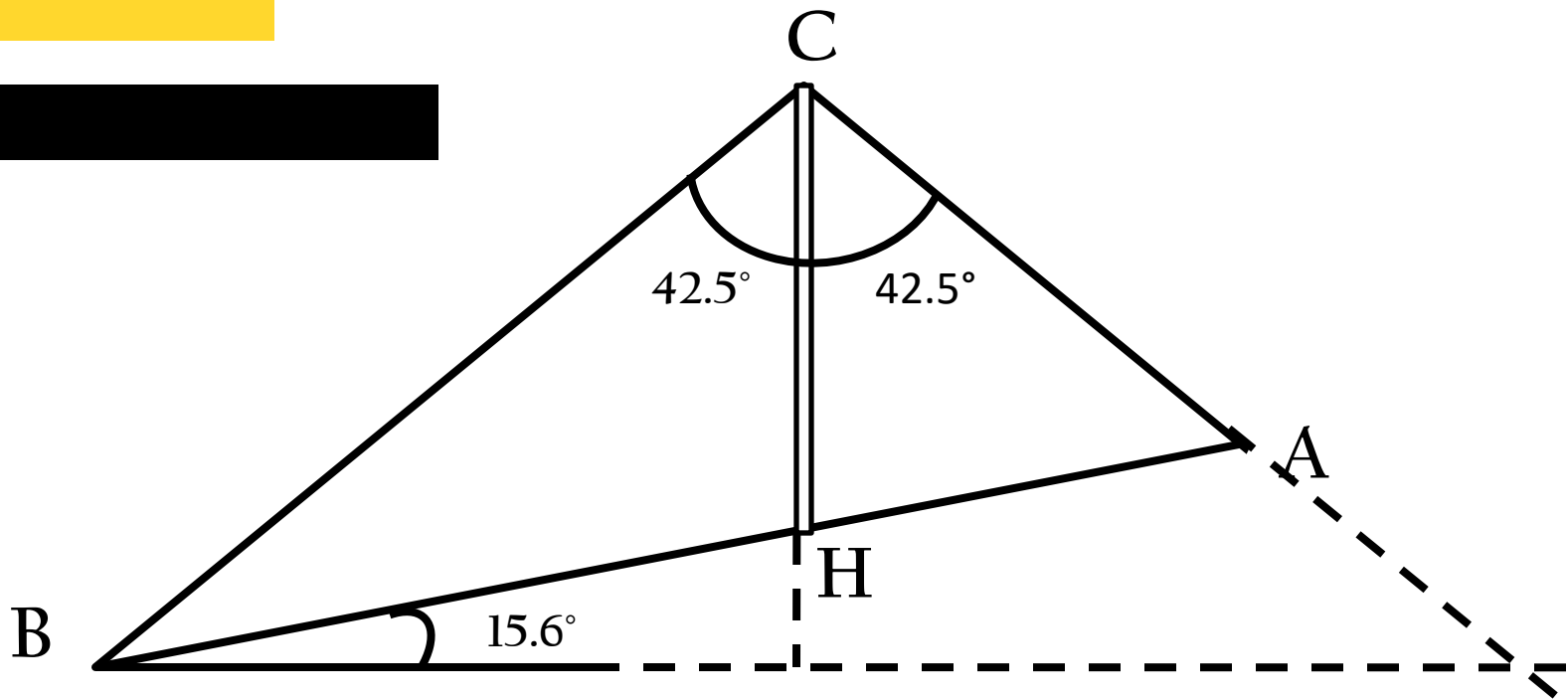


**BROZZI  
CHIAPPINO  
D'ETTORRE  
DI CARLO  
GIAMMARINO  
MELCHIORRE**

**THE LAW OF  
SINES**

A 71.6-m-high antenna mast is to be placed on sloping ground with the cables making an angle of  $42.5^\circ$  with the top of the mast. Find the length of each cable.





Let's imagine to extend the sides of the triangle to create an isosceles triangle.

We can divide this new triangle in two right triangles extending CH.

Now we can find the angle  $\beta$ :

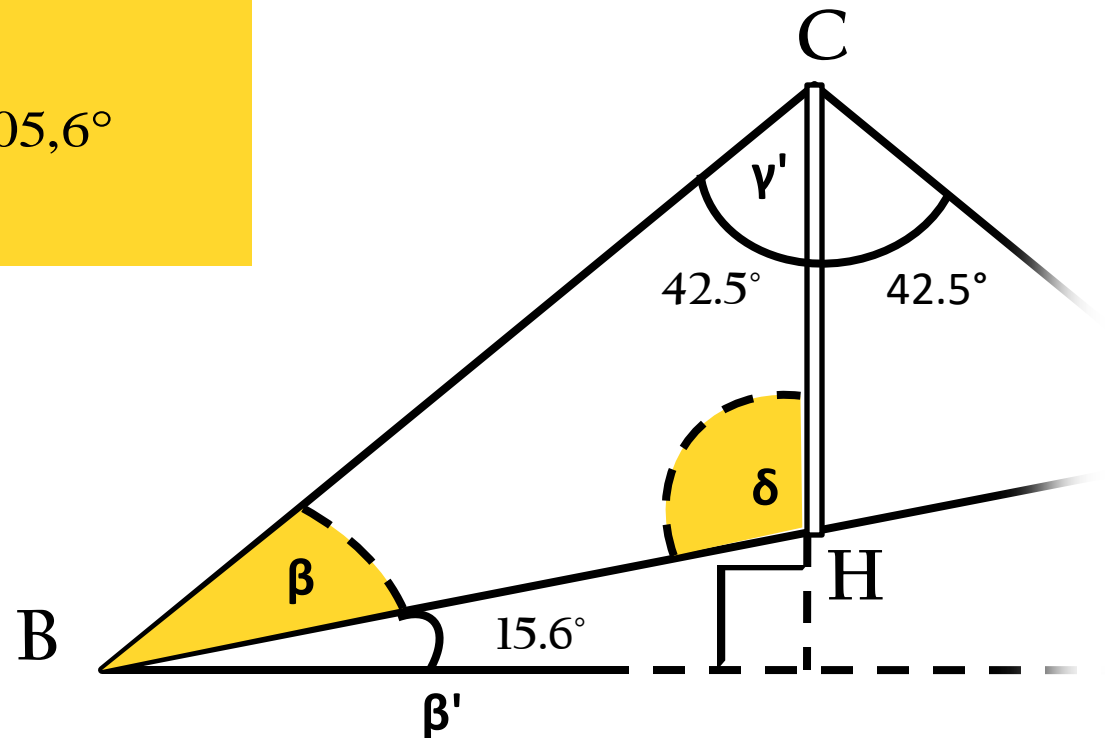
$$(\beta + \beta') = 180^\circ - (\gamma' + 90^\circ) = 47,5^\circ$$

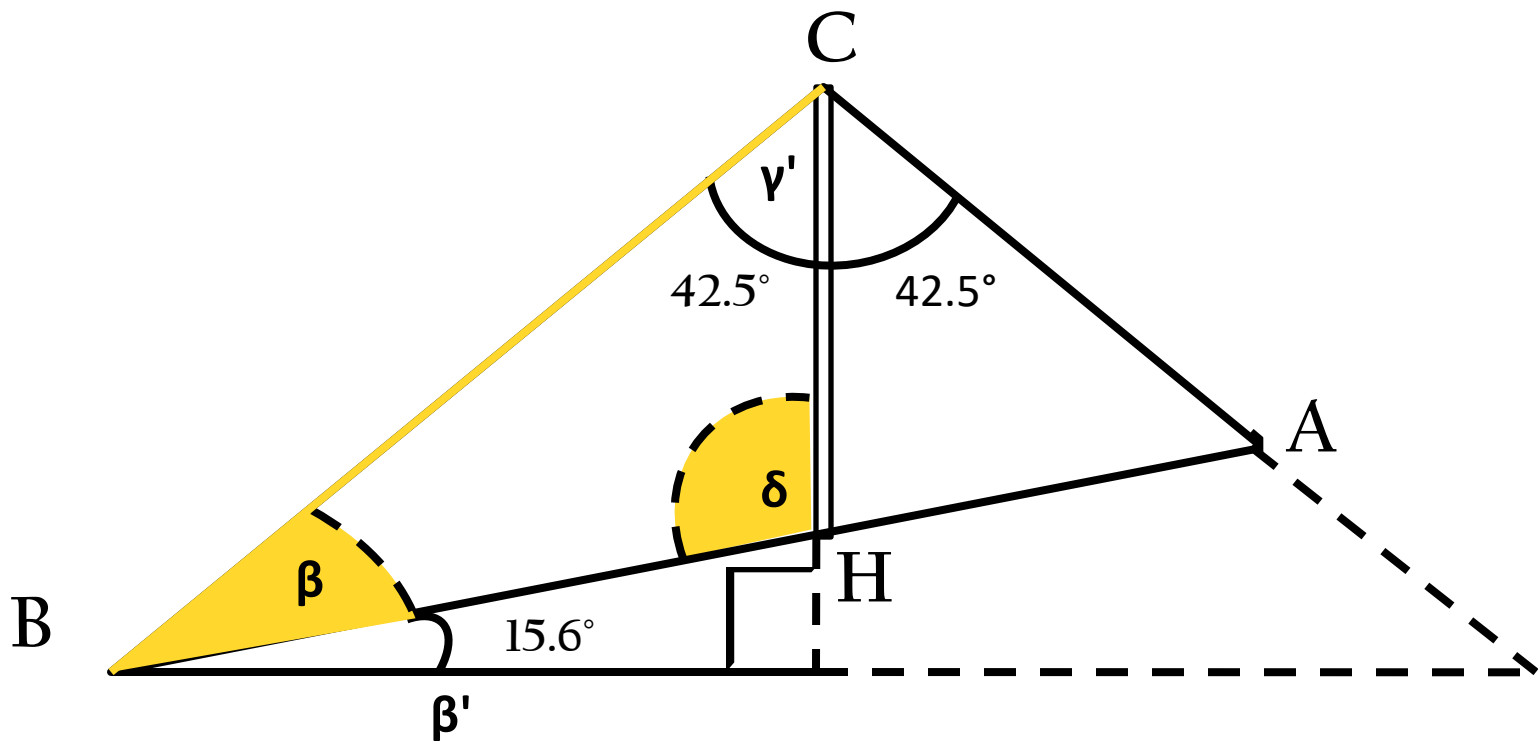
$$\beta = (\beta + \beta') - \beta' = 31,9^\circ$$

With the same process we can find the angle  $\delta$ :

$\delta$ :

$$\delta = 180^\circ - \gamma' - \beta = 105,6^\circ$$





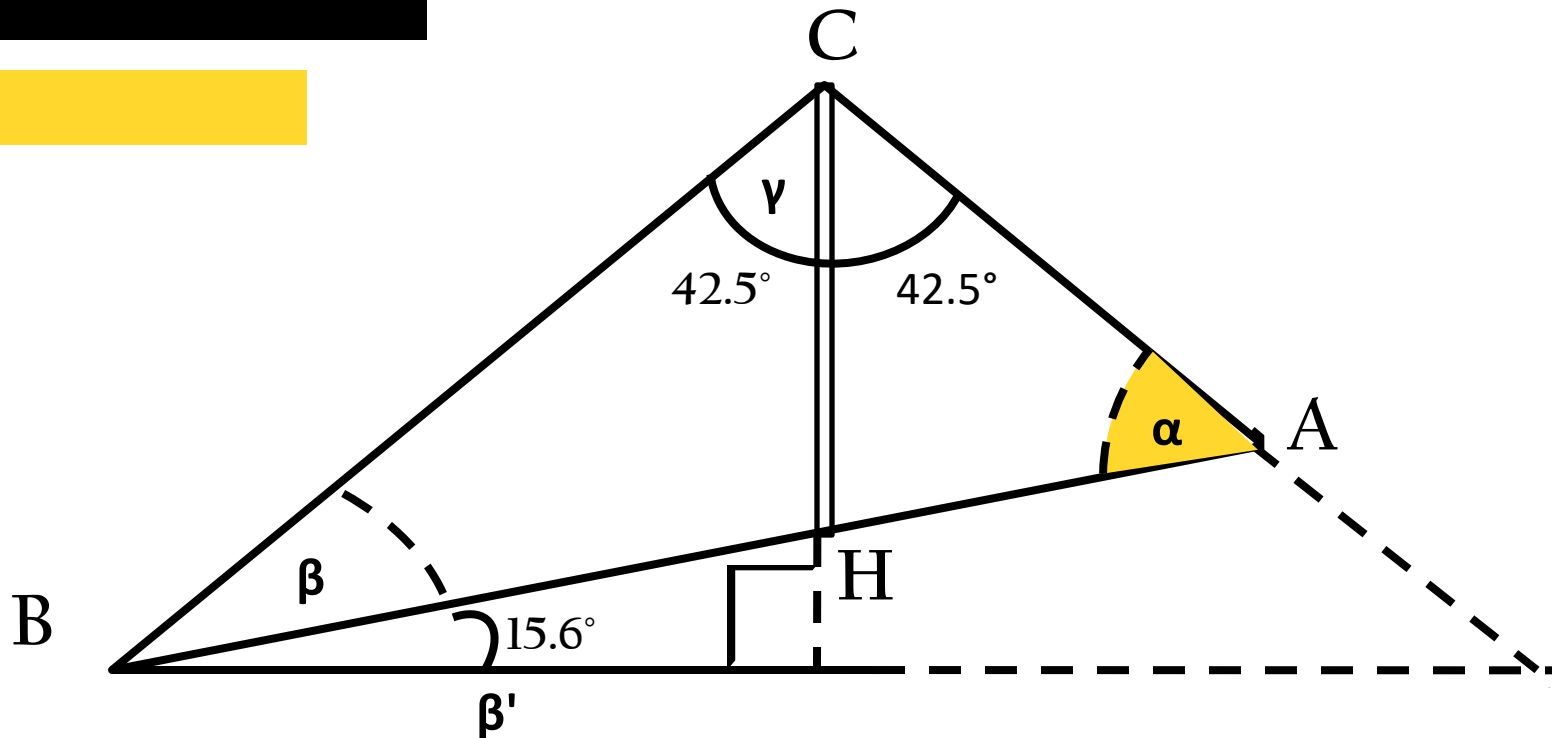
Now, using the Law of Sines, we can find the side CB:

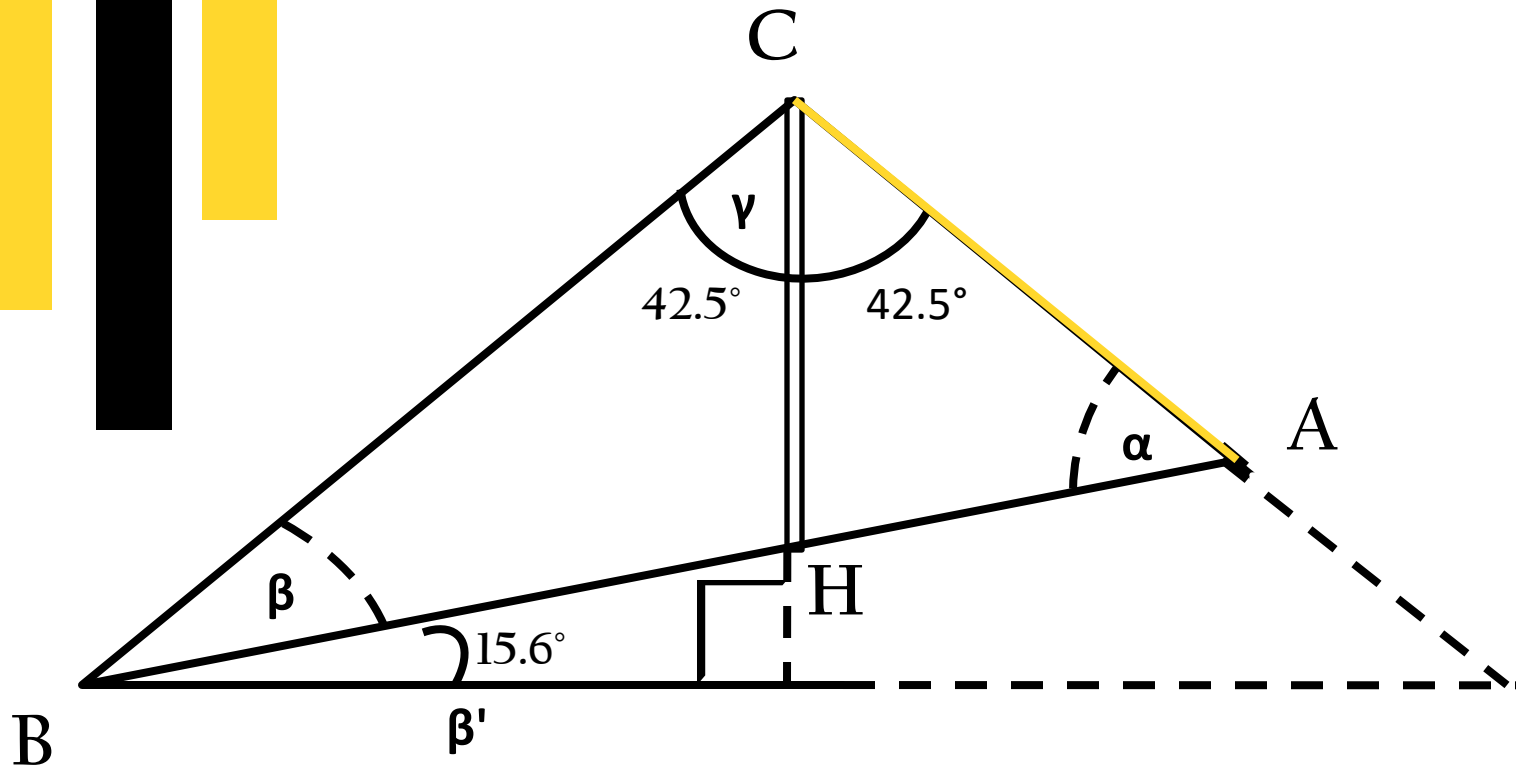
$$\frac{CH}{\sin \beta} = \frac{CB}{\sin \delta} \Rightarrow CB = CH \frac{\sin \delta}{\sin \beta} \Rightarrow CB = 71,6 \frac{0,96}{0,53} = 130 \text{ cm}$$

As we know the angles  $\beta$  and  $\gamma$ , we can find  $\alpha$ :

$$\alpha = 180^\circ - \beta - \gamma$$

$$\alpha = 180^\circ - 31,9^\circ - 85^\circ = 63,1^\circ$$





Last but not least, we can find CA using the Law of the Sines:

$$\frac{CA}{\sin\beta} = \frac{CB}{\sin\alpha} \Rightarrow CA = CB \frac{\sin\beta}{\sin\alpha} \Rightarrow CA = 130 \frac{0,53}{0,89} = 77,4\text{cm}$$